

(000)+ (1/2 1/2 0)+

Multiplicity Site-symmetry group

Coordinates

8

1

$xyz, xy^{1/2+z}, \overline{xyz}, \overline{xy^{1/2-z}}$

4

2

$0y^{1/4}, 0\overline{y^{3/4}}$

4

$\overline{1}$

$000, 00^{1/2}$

4

$\overline{1}$

$0^{1/2}0, 0^{1/2}1/2$

4

$\overline{1}$

$\overbrace{1/4^{1/4}0, 1/4^{3/4}1/2, (3/4^{3/4}0, 3/4^{1/4}1/2)}$

Related by (1/2 1/2 0)+, we do not write these coordinates explicitly

4

$\overline{1}$

$\underbrace{1/4^{3/4}0, 1/4^{1/4}1/2}$

$C2/c$

C_{2h}^6

$2/m$

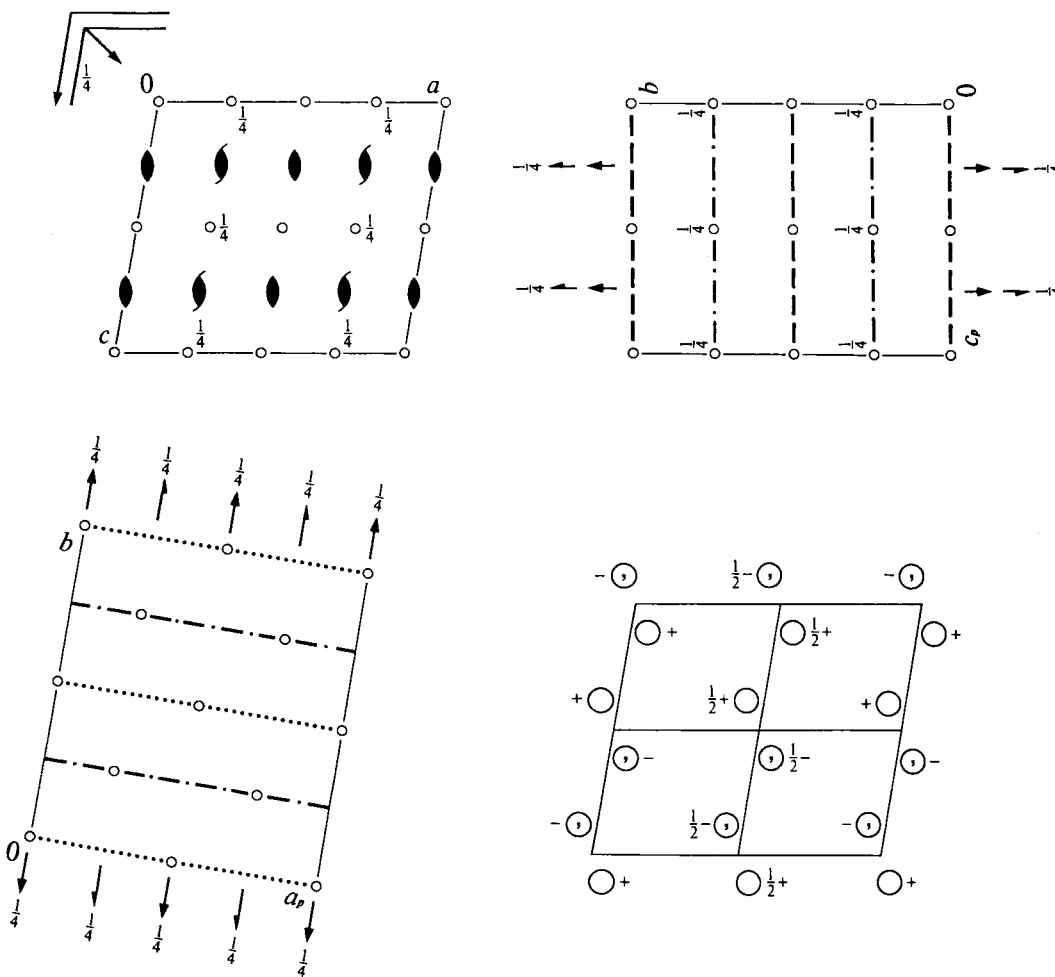
Monoclinic

No. 15

$C12/c1$

Patterson symmetry $C12/m1$

UNIQUE AXIS b , CELL CHOICE 1



Origin at $\bar{1}$ on glide plane c

Asymmetric unit $0 \leq x \leq \frac{1}{2}; 0 \leq y \leq \frac{1}{2}; 0 \leq z \leq \frac{1}{2}$

Symmetry operations

For $(0,0,0)+$ set

- | | | | |
|-------|---------------------------------|-----------------------------|-----------------------|
| (1) 1 | (2) $2 \quad 0, y, \frac{1}{4}$ | (3) $\bar{1} \quad 0, 0, 0$ | (4) $c \quad x, 0, z$ |
|-------|---------------------------------|-----------------------------|-----------------------|

For $(\frac{1}{2}, \frac{1}{2}, 0)+$ set

- | | | | |
|--------------------------------------|--|---|--|
| (1) $t(\frac{1}{2}, \frac{1}{2}, 0)$ | (2) $2(0, \frac{1}{2}, 0) \quad \frac{1}{4}, y, \frac{1}{4}$ | (3) $\bar{1} \quad \frac{1}{4}, \frac{1}{4}, 0$ | (4) $n(\frac{1}{2}, 0, \frac{1}{2}) \quad x, \frac{1}{4}, z$ |
|--------------------------------------|--|---|--|

Generators selected (1); $t(1,0,0)$; $t(0,1,0)$; $t(0,0,1)$; $t(\frac{1}{2},\frac{1}{2},0)$; (2); (3)

Positions

Multiplicity, Wyckoff letter, Site symmetry	Coordinates				Reflection conditions
	(0,0,0)+ $(\frac{1}{2},\frac{1}{2},0)$ +				General:
8 <i>f</i> 1	(1) x,y,z	(2) $\bar{x},y,\bar{z}+\frac{1}{2}$	(3) \bar{x},\bar{y},\bar{z}	(4) $x,\bar{y},z+\frac{1}{2}$	$hkl : h+k=2n$ $h0l : h,l=2n$ $0kl : k=2n$ $hk0 : h+k=2n$ $0k0 : k=2n$ $h00 : h=2n$ $00l : l=2n$
					Special: as above, plus
4 <i>e</i> 2	$0,y,\frac{1}{4}$	$0,\bar{y},\frac{3}{4}$			no extra conditions
4 <i>d</i> $\bar{1}$	$\frac{1}{4},\frac{1}{4},\frac{1}{2}$	$\frac{3}{4},\frac{1}{4},0$			$hkl : k+l=2n$
4 <i>c</i> $\bar{1}$	$\frac{1}{4},\frac{1}{4},0$	$\frac{3}{4},\frac{1}{4},\frac{1}{2}$			$hkl : k+l=2n$
4 <i>b</i> $\bar{1}$	$0,\frac{1}{2},0$	$0,\frac{1}{2},\frac{1}{2}$			$hkl : l=2n$
4 <i>a</i> $\bar{1}$	$0,0,0$	$0,0,\frac{1}{2}$			$hkl : l=2n$

Symmetry of special projections

Along [001] $c2mm$
 $\mathbf{a}' = \mathbf{a}_p$ $\mathbf{b}' = \mathbf{b}$
 Origin at 0,0,z

Along [100] $p2gm$
 $\mathbf{a}' = \frac{1}{2}\mathbf{b}$ $\mathbf{b}' = \mathbf{c}_p$
 Origin at x,0,0

Along [010] $p2$
 $\mathbf{a}' = \frac{1}{2}\mathbf{c}$ $\mathbf{b}' = \frac{1}{2}\mathbf{a}$
 Origin at 0,y,0

Maximal non-isomorphic subgroups

I	[2] $C1c1$ (Cc , 9)	(1; 4)+
	[2] $C121$ ($C2$, 5)	(1; 2)+
	[2] $C\bar{1}$ ($P\bar{1}$, 2)	(1; 3)+
IIa	[2] $P12_1/n1$ ($P2_1/c$, 14)	1; 3; (2; 4) + $(\frac{1}{2},\frac{1}{2},0)$
	[2] $P12_1/c1$ ($P2_1/c$, 14)	1; 4; (2; 3) + $(\frac{1}{2},\frac{1}{2},0)$
	[2] $P12/c1$ ($P2/c$, 13)	1; 2; 3; 4
	[2] $P12/n1$ ($P2/c$, 13)	1; 2; (3; 4) + $(\frac{1}{2},\frac{1}{2},0)$
IIb	none	

Maximal isomorphic subgroups of lowest index

IIc [3] $C12/c1$ ($\mathbf{b}' = 3\mathbf{b}$) ($C2/c$, 15); [3] $C12/c1$ ($\mathbf{c}' = 3\mathbf{c}$) ($C2/c$, 15);
 [3] $C12/c1$ ($\mathbf{a}' = 3\mathbf{a}$ or $\mathbf{a}' = 3\mathbf{a}, \mathbf{c}' = -\mathbf{a} + \mathbf{c}$ or $\mathbf{a}' = 3\mathbf{a}, \mathbf{c}' = \mathbf{a} + \mathbf{c}$) ($C2/c$, 15)

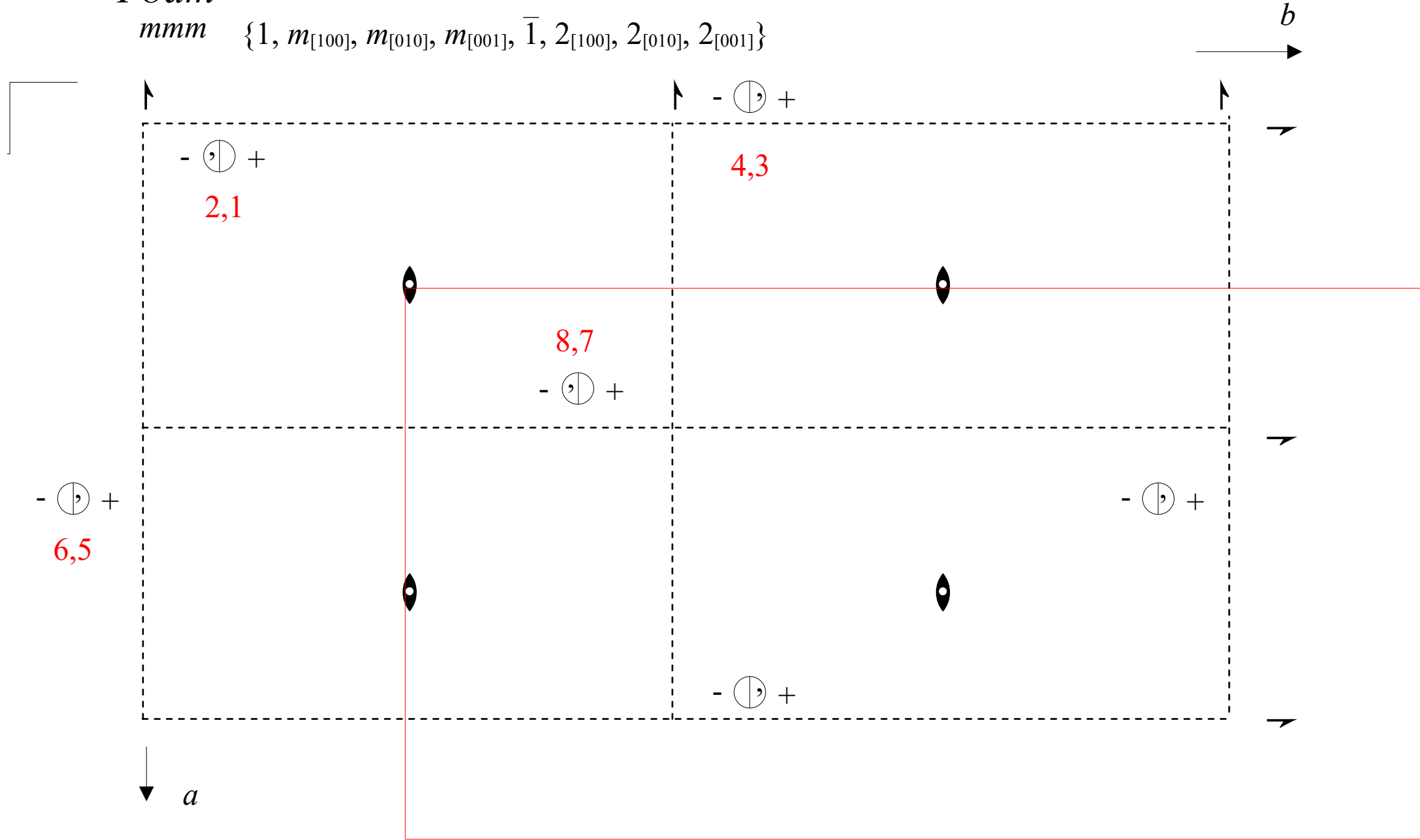
Minimal non-isomorphic supergroups

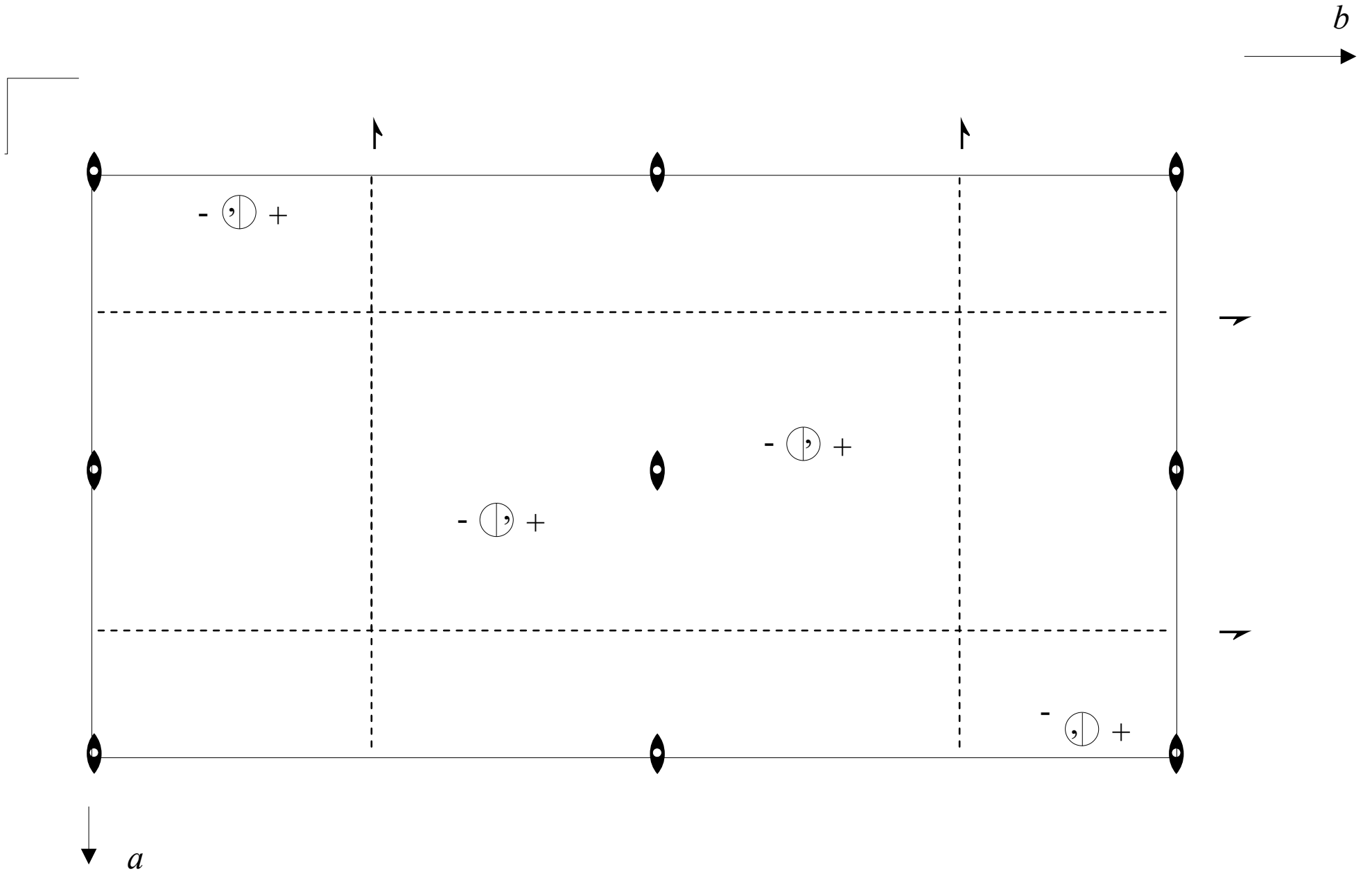
I	[2] $Cmcm$ (63); [2] $Cmce$ (64); [2] $Cccm$ (66); [2] $Ccce$ (68); [2] $Fddd$ (70); [2] $Ibam$ (72); [2] $Ibca$ (73); [2] $Imma$ (74); [2] $I4/a$ (88); [3] $P\bar{3}1c$ (163); [3] $P\bar{3}c1$ (165); [3] $R\bar{3}c$ (167)
II	[2] $F12/m1$ ($C2/m$, 12); [2] $C12/m1$ ($\mathbf{c}' = \frac{1}{2}\mathbf{c}$) ($C2/m$, 12); [2] $P12/c1$ ($\mathbf{a}' = \frac{1}{2}\mathbf{a}, \mathbf{b}' = \frac{1}{2}\mathbf{b}$) ($P2/c$, 13)

$[100]$ $[010]$ $[001]$

$Pbam$

mmm $\{1, m_{[100]}, m_{[010]}, m_{[001]}, \bar{1}, 2_{[100]}, 2_{[010]}, 2_{[001]}\}$





Multiplicity	Site-symmetry group	Coordinates
8	1	$xyz, xy\bar{z}, \frac{1}{2}+x, \frac{1}{2}-yz, \frac{1}{2}+x\frac{1}{2}-y\bar{z}, \overline{xyz}, \overline{xy\bar{z}}, \frac{1}{2}-x\frac{1}{2}+yz, \frac{1}{2}-x\frac{1}{2}+y\bar{z}$
4	$..m$	$xy0, \frac{1}{2}+x, \frac{1}{2}-y0, \overline{xy0}, \frac{1}{2}-x\frac{1}{2}+y0$
4	$..m$	$xy\frac{1}{2}, \frac{1}{2}+x, \frac{1}{2}-y\frac{1}{2}, \overline{xy\frac{1}{2}}, \frac{1}{2}-x\frac{1}{2}+y\frac{1}{2}$
4	$..2$	$00z, 00\bar{z}, \frac{1}{2}\frac{1}{2}z, \frac{1}{2}\frac{1}{2}\bar{z}$
4	$..2$	$\frac{1}{2}0z, \frac{1}{2}0\bar{z}, 0\frac{1}{2}z, 0\frac{1}{2}\bar{z}$
2	$..2/m$	$000, \frac{1}{2}\frac{1}{2}0$
2	$..2/m$	$00\frac{1}{2}, \frac{1}{2}\frac{1}{2}\frac{1}{2}$
2	$..2/m$	$\frac{1}{2}00, 0\frac{1}{2}0$
2	$..2/m$	$\frac{1}{2}0\frac{1}{2}, 0\frac{1}{2}\frac{1}{2}$

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & \bar{1} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} x \\ \bar{y} \\ z \end{bmatrix}$$

Pbam

D_{2h}^9

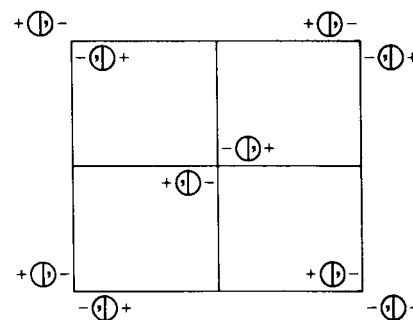
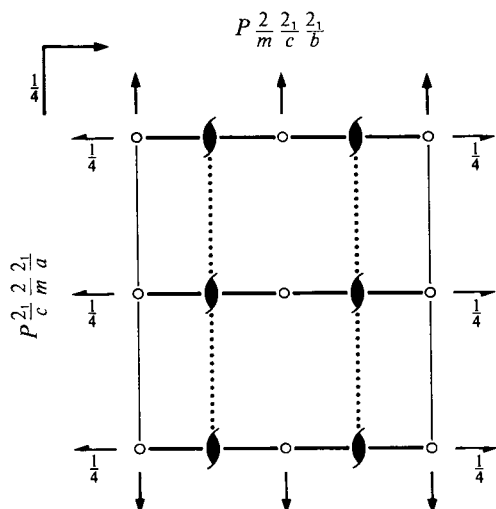
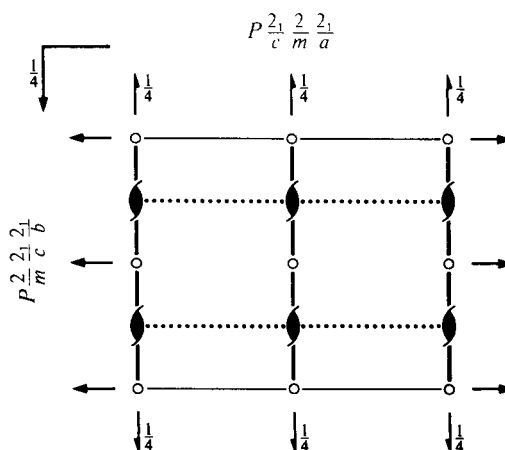
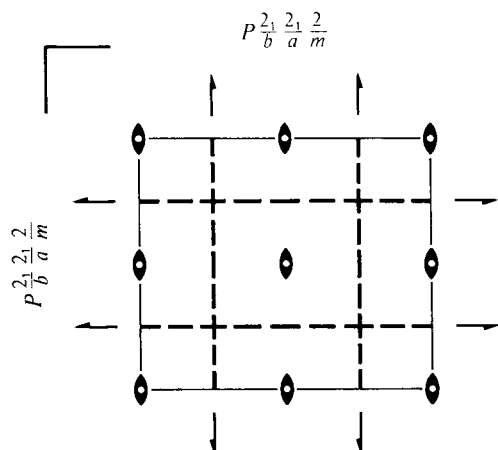
mmm

Orthorhombic

No. 55

$P 2_1/b 2_1/a 2/m$

Patterson symmetry *Pmmm*



Origin at centre ($2/m$)

Asymmetric unit $0 \leq x \leq \frac{1}{2}; 0 \leq y \leq \frac{1}{2}; 0 \leq z \leq \frac{1}{2}$

Symmetry operations

- | | | | |
|-----------------------|-----------------|--|--|
| (1) 1 | (2) 2 $0,0,z$ | (3) $2(0, \frac{1}{2}, 0)$ $\frac{1}{4}, y, 0$ | (4) $2(\frac{1}{2}, 0, 0)$ $x, \frac{1}{4}, 0$ |
| (5) $\bar{1}$ $0,0,0$ | (6) m $x,y,0$ | (7) a $x, \frac{1}{4}, z$ | (8) b $\frac{1}{4}, y, z$ |

Generators selected (1); $t(1,0,0)$; $t(0,1,0)$; $t(0,0,1)$; (2); (3); (5)

Positions

Multiplicity, Wyckoff letter, Site symmetry	Coordinates				Reflection conditions
8 <i>i</i> 1	(1) x, y, z (5) $\bar{x}, \bar{y}, \bar{z}$	(2) \bar{x}, \bar{y}, z (6) x, y, \bar{z}	(3) $\bar{x} + \frac{1}{2}, y + \frac{1}{2}, \bar{z}$ (7) $x + \frac{1}{2}, \bar{y} + \frac{1}{2}, z$	(4) $x + \frac{1}{2}, \bar{y} + \frac{1}{2}, \bar{z}$ (8) $\bar{x} + \frac{1}{2}, y + \frac{1}{2}, z$	General: $Ok\bar{l} : k = 2n$ $h0l : h = 2n$ $h00 : h = 2n$ $0k0 : k = 2n$ Special: as above, plus
4 <i>h</i> .. <i>m</i>	$x, y, \frac{1}{2}$	$\bar{x}, \bar{y}, \frac{1}{2}$	$\bar{x} + \frac{1}{2}, y + \frac{1}{2}, \frac{1}{2}$	$x + \frac{1}{2}, \bar{y} + \frac{1}{2}, \frac{1}{2}$	no extra conditions
4 <i>g</i> .. <i>m</i>	$x, y, 0$	$\bar{x}, \bar{y}, 0$	$\bar{x} + \frac{1}{2}, y + \frac{1}{2}, 0$	$x + \frac{1}{2}, \bar{y} + \frac{1}{2}, 0$	no extra conditions
4 <i>f</i> .. 2	$0, \frac{1}{2}, z$	$\frac{1}{2}, 0, \bar{z}$	$0, \frac{1}{2}, \bar{z}$	$\frac{1}{2}, 0, z$	$hkl : h + k = 2n$
4 <i>e</i> .. 2	$0, 0, z$	$\frac{1}{2}, \frac{1}{2}, \bar{z}$	$0, 0, \bar{z}$	$\frac{1}{2}, \frac{1}{2}, z$	$hkl : h + k = 2n$
2 <i>d</i> .. $2/m$	$0, \frac{1}{2}, \frac{1}{2}$	$\frac{1}{2}, 0, \frac{1}{2}$			$hkl : h + k = 2n$
2 <i>c</i> .. $2/m$	$0, \frac{1}{2}, 0$	$\frac{1}{2}, 0, 0$			$hkl : h + k = 2n$
2 <i>b</i> .. $2/m$	$0, 0, \frac{1}{2}$	$\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$			$hkl : h + k = 2n$
2 <i>a</i> .. $2/m$	$0, 0, 0$	$\frac{1}{2}, \frac{1}{2}, 0$			$hkl : h + k = 2n$

Symmetry of special projections

Along [001] $p2gg$
 $\mathbf{a}' = \mathbf{a}$ $\mathbf{b}' = \mathbf{b}$
Origin at 0, 0, z

Along [100] $p2mm$
 $\mathbf{a}' = \frac{1}{2}\mathbf{b}$ $\mathbf{b}' = \mathbf{c}$
Origin at $x, 0, 0$

Along [010] $p2mm$
 $\mathbf{a}' = \mathbf{c}$ $\mathbf{b}' = \frac{1}{2}\mathbf{a}$
Origin at 0, $y, 0$

Maximal non-isomorphic subgroups

I [2] $Pba2$ (32) 1; 2; 7; 8
 [2] $Pb2_1m$ ($Pmc2_1$, 26) 1; 3; 6; 8
 [2] $P2_1am$ ($Pmc2_1$, 26) 1; 4; 6; 7
 [2] $P2_12_12$ (18) 1; 2; 3; 4
 [2] $P12_1/a1$ ($P2_1/c$, 14) 1; 3; 5; 7
 [2] $P2_1/b11$ ($P2_1/c$, 14) 1; 4; 5; 8
 [2] $P112/m$ ($P2/m$, 10) 1; 2; 5; 6

IIa none

IIb [2] $Pnam$ ($\mathbf{c}' = 2\mathbf{c}$) ($Pnma$, 62); [2] $Pbnm$ ($\mathbf{c}' = 2\mathbf{c}$) ($Pnma$, 62); [2] $Pnnm$ ($\mathbf{c}' = 2\mathbf{c}$) (58)

Maximal isomorphic subgroups of lowest index

IIc [2] $Pbam$ ($\mathbf{c}' = 2\mathbf{c}$) (55); [3] $Pbam$ ($\mathbf{a}' = 3\mathbf{a}$ or $\mathbf{b}' = 3\mathbf{b}$) (55)

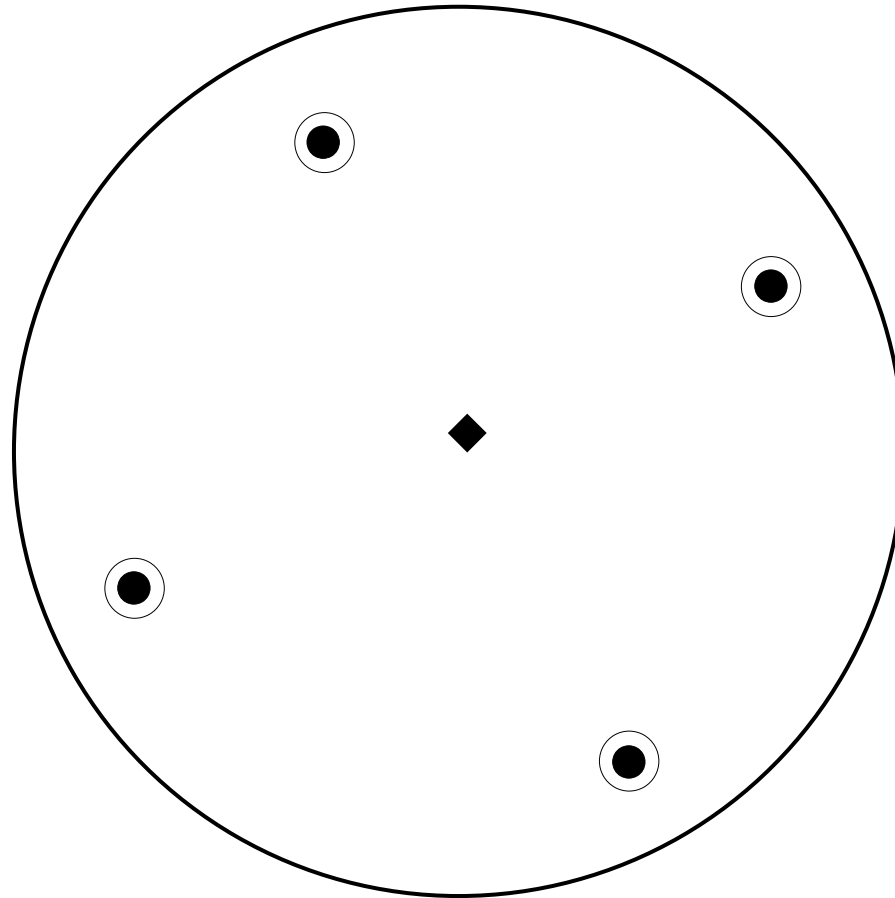
Minimal non-isomorphic supergroups

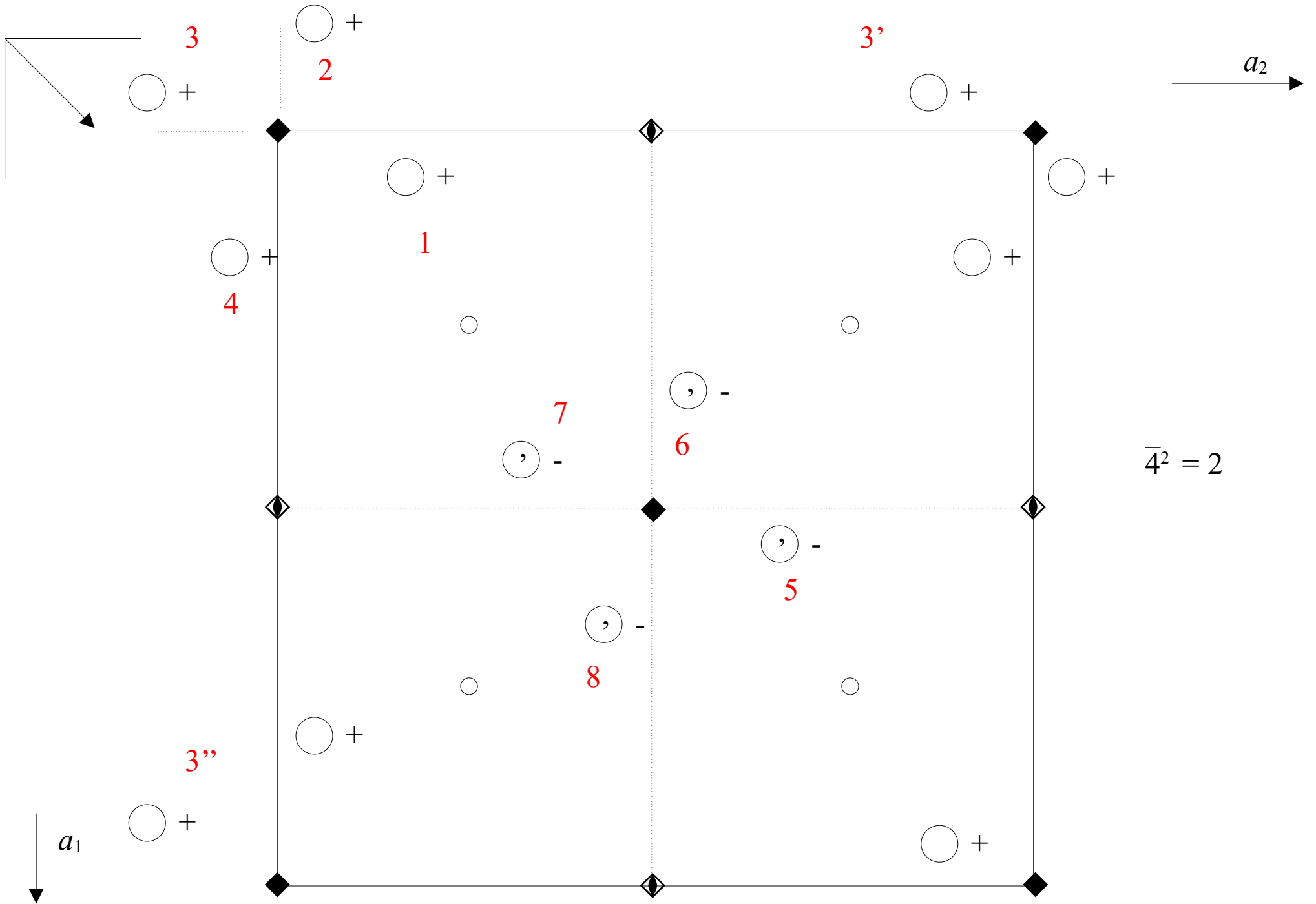
I [2] $P4/mbm$ (127); [2] $P4_2/mbc$ (135)

II [2] $Aeam$ ($Cmce$, 64); [2] $Bbem$ ($Cmce$, 64); [2] $Cmmm$ (65); [2] $Ibam$ (72); [2] $Pbmm$ ($\mathbf{a}' = \frac{1}{2}\mathbf{a}$) ($Pmma$, 51);
 [2] $Pmam$ ($\mathbf{b}' = \frac{1}{2}\mathbf{b}$) ($Pmma$, 51)

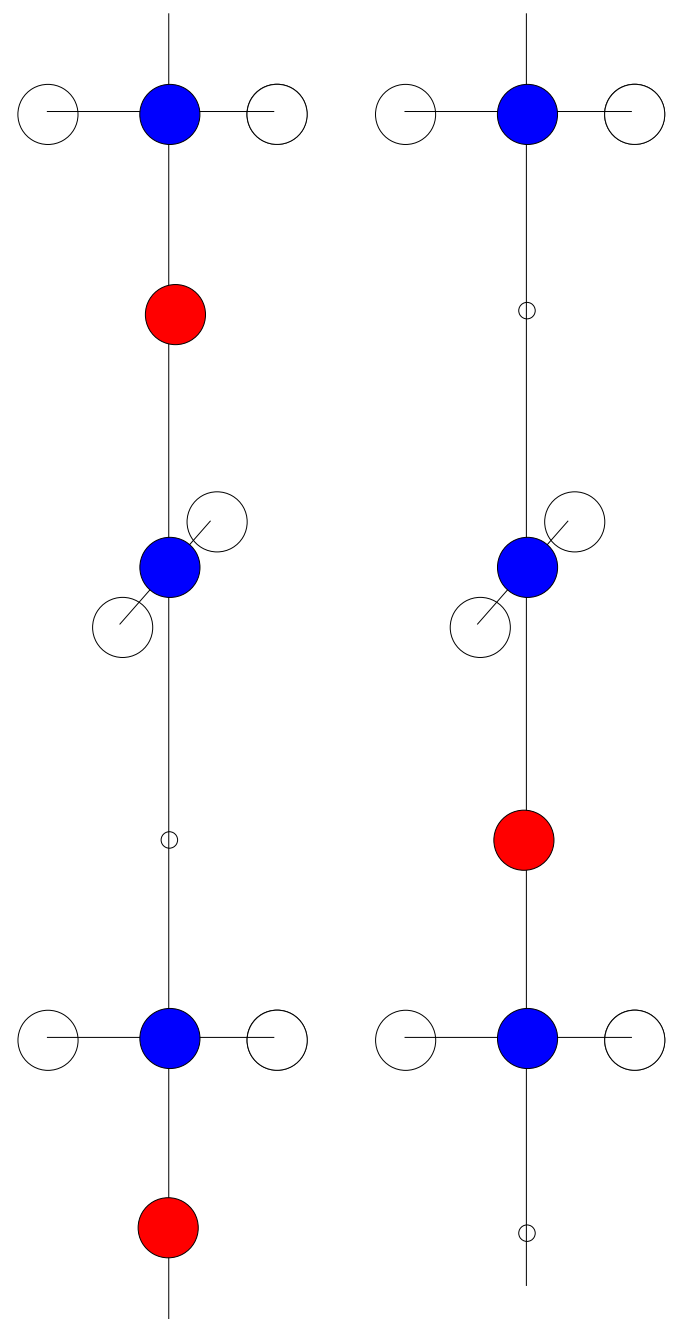
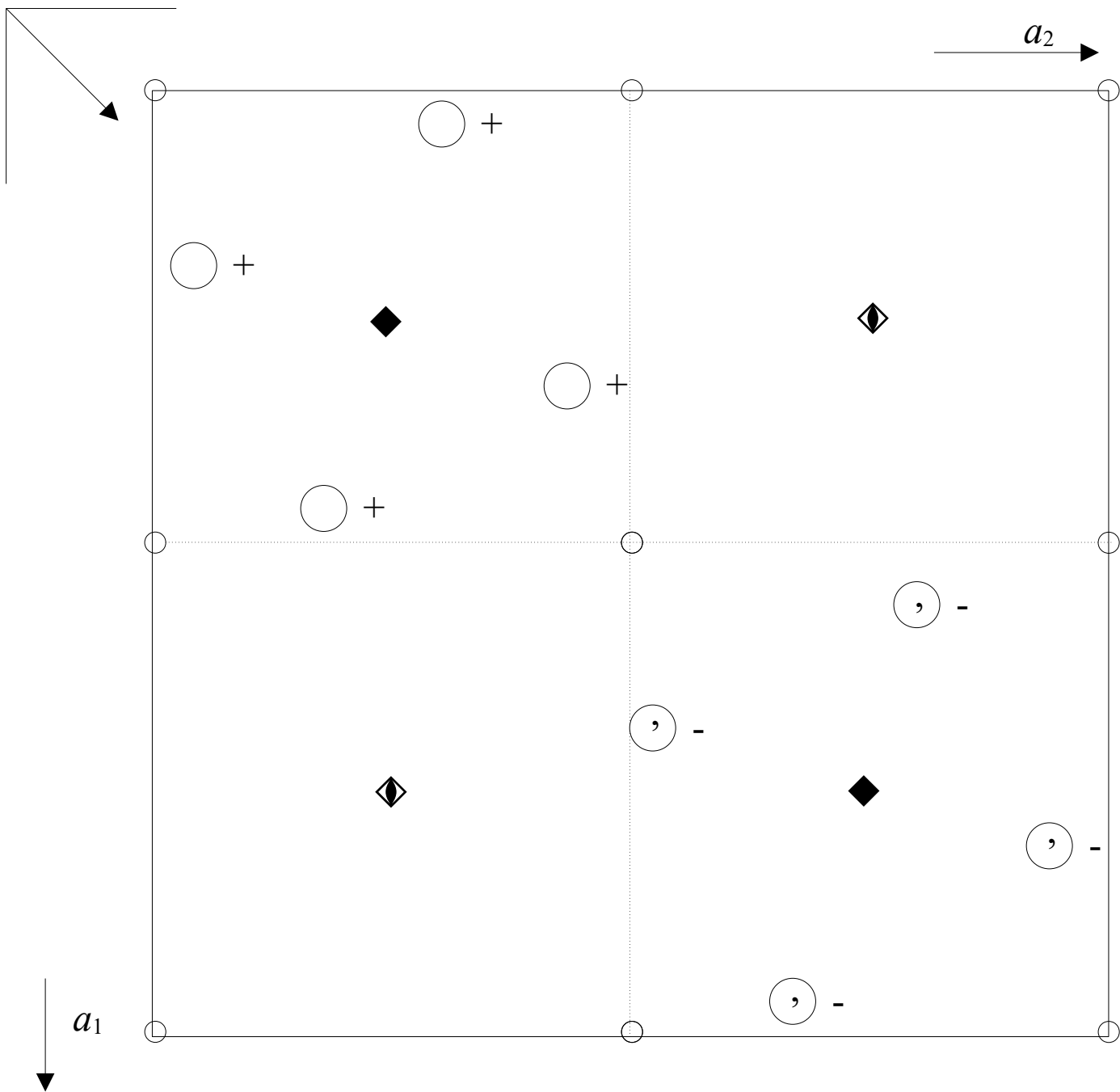
$P4/n \longrightarrow 4/m$

$[001] \langle 100 \rangle \langle 1\bar{1}0 \rangle$





$$\bar{4}^2 = 2$$



Multiplicity	Site-symmetry group	Coordinates
8	1	$\underline{x}, \underline{y}, \underline{z}; \underline{y}, \frac{1}{2} - \underline{x}, \underline{z}; \frac{1}{2} - \underline{x}, \frac{1}{2} - \underline{y}, \underline{z}; \frac{1}{2} - \underline{y}, \underline{x}, \underline{z}$ $\underline{x}, \underline{y}, \underline{z}; \underline{y}, \frac{1}{2} + \underline{x}, \underline{z}; \frac{1}{2} + \underline{x}, \frac{1}{2} + \underline{y}, \underline{z}; \frac{1}{2} + \underline{y}, \underline{x}, \underline{z}$
2	4..	$\frac{1}{4}, \frac{1}{4}, \underline{z}; \frac{3}{4}, \frac{3}{4}, \bar{\underline{z}}$
4	2..	$\frac{1}{4}, \frac{3}{4}, \underline{z}; \frac{3}{4}, \frac{1}{4}, \underline{z}; \frac{3}{4}, \frac{1}{4}, \bar{\underline{z}}; \frac{1}{4}, \frac{3}{4}, \bar{\underline{z}};$
2	$\bar{4}..$	$\frac{1}{4}, \frac{3}{4}, \underline{0}; \frac{3}{4}, \frac{1}{4}, \underline{0}$
2	$\bar{4}..$	$\frac{1}{4}, \frac{3}{4}, \frac{1}{2}; \frac{3}{4}, \frac{1}{4}, \frac{1}{2}$
4	$\bar{1}$	$000, 0\frac{1}{2}0, \frac{1}{2}\frac{1}{2}0, \frac{1}{2}00$
4	$\bar{1}$	$00\frac{1}{2}, 0\frac{1}{2}\frac{1}{2}, \frac{1}{2}\frac{1}{2}\frac{1}{2}, \frac{1}{2}0\frac{1}{2}$

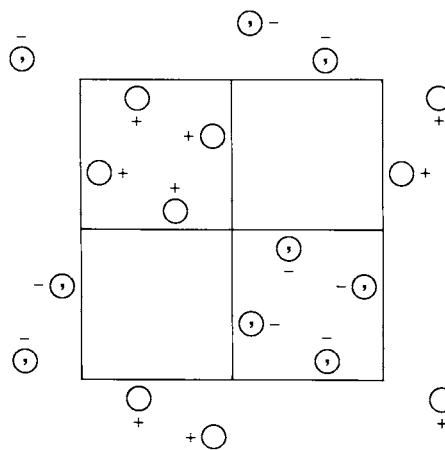
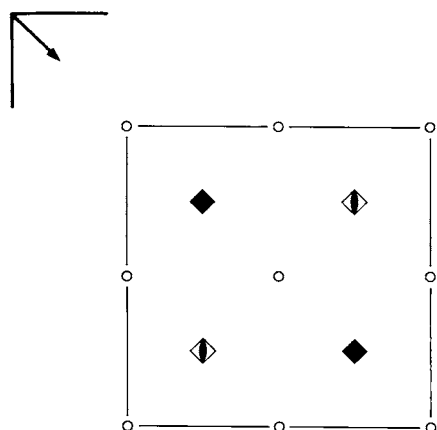
$P4/n$ C_{4h}^3 $4/m$

Tetragonal

No. 85

 $P4/n$ Patterson symmetry $P4/m$

ORIGIN CHOICE 2



Origin at $\bar{1}$ on n , at $\frac{1}{4}, -\frac{1}{4}, 0$ from $\bar{4}$

Asymmetric unit $-\frac{1}{4} \leq x \leq \frac{1}{4}; -\frac{1}{4} \leq y \leq \frac{1}{4}; 0 \leq z \leq \frac{1}{2}$

Symmetry operations

- | | | | |
|-----------------------|--|--|--|
| (1) 1 | (2) $2 \frac{1}{4}, \frac{1}{4}, z$ | (3) $4^+ \frac{1}{4}, \frac{1}{4}, z$ | (4) $4^- \frac{1}{4}, \frac{1}{4}, z$ |
| (5) $\bar{1} 0, 0, 0$ | (6) $n(\frac{1}{2}, \frac{1}{2}, 0) x, y, 0$ | (7) $\bar{4}^+ \frac{1}{4}, -\frac{1}{4}, z; \frac{1}{4}, -\frac{1}{4}, 0$ | (8) $\bar{4}^- -\frac{1}{4}, \frac{1}{4}, z; -\frac{1}{4}, \frac{1}{4}, 0$ |

Generators selected (1); $t(1,0,0)$; $t(0,1,0)$; $t(0,0,1)$; (2); (3); (5)

Positions

Multiplicity, Wyckoff letter, Site symmetry		Coordinates				Reflection conditions
8	<i>g</i> 1	(1) x, y, z (5) $\bar{x}, \bar{y}, \bar{z}$	(2) $\bar{x} + \frac{1}{2}, \bar{y} + \frac{1}{2}, z$ (6) $x + \frac{1}{2}, y + \frac{1}{2}, \bar{z}$	(3) $\bar{y} + \frac{1}{2}, x, z$ (7) $y + \frac{1}{2}, \bar{x}, \bar{z}$	(4) $y, \bar{x} + \frac{1}{2}, z$ (8) $\bar{y}, x + \frac{1}{2}, \bar{z}$	General: $hkl : h + k = 2n$ $h00 : h = 2n$ Special: as above, plus $hkl : h + k = 2n$ $hkl : h, k = 2n$ $hkl : h, k = 2n$ no extra conditions $hkl : h + k = 2n$ $hkl : h + k = 2n$
4	<i>f</i> 2..	$\frac{1}{4}, \frac{3}{4}, z$	$\frac{3}{4}, \frac{1}{4}, z$	$\frac{3}{4}, \frac{1}{4}, \bar{z}$	$\frac{1}{4}, \frac{3}{4}, \bar{z}$	
4	<i>e</i> $\bar{1}$	$0, 0, \frac{1}{2}$	$\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$	$\frac{1}{2}, 0, \frac{1}{2}$	$0, \frac{1}{2}, \frac{1}{2}$	
4	<i>d</i> $\bar{1}$	$0, 0, 0$	$\frac{1}{2}, \frac{1}{2}, 0$	$\frac{1}{2}, 0, 0$	$0, \frac{1}{2}, 0$	
2	<i>c</i> 4..	$\frac{1}{4}, \frac{1}{4}, z$	$\frac{3}{4}, \frac{3}{4}, \bar{z}$			
2	<i>b</i> $\bar{4}$..	$\frac{1}{4}, \frac{3}{4}, \frac{1}{2}$	$\frac{3}{4}, \frac{1}{4}, \frac{1}{2}$			
2	<i>a</i> $\bar{4}$..	$\frac{1}{4}, \frac{3}{4}, 0$	$\frac{3}{4}, \frac{1}{4}, 0$			

Symmetry of special projections

Along [001] $p4$

$$\mathbf{a}' = \frac{1}{2}(\mathbf{a} - \mathbf{b}) \quad \mathbf{b}' = \frac{1}{2}(\mathbf{a} + \mathbf{b})$$

Origin at $\frac{1}{4}, \frac{1}{4}, z$

Along [100] $p2mg$

$$\mathbf{a}' = \mathbf{b} \quad \mathbf{b}' = \mathbf{c}$$

Origin at $x, 0, 0$

Along [110] $p2mm$

$$\mathbf{a}' = \frac{1}{2}(-\mathbf{a} + \mathbf{b}) \quad \mathbf{b}' = \mathbf{c}$$

Origin at $x, x, 0$

Maximal non-isomorphic subgroups

I	[2] $P\bar{4}$ (81)	1; 2; 7; 8
	[2] $P4$ (75)	1; 2; 3; 4
	[2] $P2/n$ ($P2/c$, 13)	1; 2; 5; 6

IIa none

IIb [2] $P4_2/n$ ($c' = 2c$) (86)

Maximal isomorphic subgroups of lowest index

IIc [2] $P4/n$ ($c' = 2c$) (85); [5] $P4/n$ ($\mathbf{a}' = \mathbf{a} + 2\mathbf{b}, \mathbf{b}' = -2\mathbf{a} + \mathbf{b}$ or $\mathbf{a}' = \mathbf{a} - 2\mathbf{b}, \mathbf{b}' = 2\mathbf{a} + \mathbf{b}$) (85)

Minimal non-isomorphic supergroups

I [2] $P4/nbm$ (125); [2] $P4/nnc$ (126); [2] $P4/nmm$ (129); [2] $P4/ncc$ (130)

II [2] $C4/m$ ($P4/m$, 83); [2] $I4/m$ (87)